UNCERTAINTY IN HISTORICAL LAND-USE RECONSTRUCTIONS WITH TOPOGRAPHIC MAPS

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ABSTRACT: The paper presents the outcomes of the uncertainty investigation of a long-term forest cover change analysis in the Polish Carpathians (nearly 20,000 km²) and Swiss Alps (nearly 10,000 km²) based on topographic maps. Following Leyk et al. (2005) all possible uncertainties are grouped into three domains – production-oriented, transformation-oriented and application-oriented. We show typical examples for each uncertainty domain, encountered during the forest cover change analysis and discuss consequences for change detection. Finally, a proposal for reliability assessment is presented.

KEY WORDS: forest cover change, uncertainty, topographic maps, the Carpathians, the Alps

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Introduction

Land-use change analysis based on cartographic information is always subject to uncertainty. The main reason is that maps are simplified models of reality (Veregin 1999). As noted by Plewe (2002), reality itself is very complex, but not uncertain, which implies that uncertainty is caused by either conceptualization, measurement or analysis processes. Map errors, differences in map instructions or interpretations cumulate with comparisons of different cartographic sources. Many methodologies and theoretical models deal with uncertainty in land-use research (Petit, Lambin 2002, Plewe 2002, Leyk et al. 2005, Pontius, Spencer 2005, Kunz 2006, Gregory, Healey

2007, Wulf, Rujner 2011, Wolski 2012), most of them, however, are tested on relatively small study areas and therefore it is not always easy to transfer their results when analysing a large portion of land.

In this study, we assess map uncertainty as a crucial aspect of a proper large-area map processing effort aiming at forest cover change analysis in the Polish Carpathians (nearly 20,000 km²) and a part of the Swiss Alps (nearly 10,000 km²) over the past 120–160 years. To do this, we had to obtain, understand, estimate and process various maps based on the best possible and relatively homogeneous data sources covering the whole studied territory. Therefore, apart from uncertainty issues, we had to cope also with map

availability and temporal coherence problems. In this paper we show crucial uncertainty issues encountered during our long-term forest cover change analysis. First, we introduce a conceptual framework of uncertainty investigation proposed by Leyk et al. (2005), and then we address this framework based on our research findings.

Conceptual framework of uncertainty investigation

Many definitions of uncertainty can be found in geospatial literature. Longley et al. (2001) define it as the acknowledgment and consideration of imprecisions in information. Zhang and Goodchild (2002) understand it as a measure of the difference between the data and the meaning attached to the data by the user. Fisher (2003) points out that uncertainty can be seen as a doubt about the information which is recorded at specific location. These definitions show the problem in a broad sense and do not refer directly to historical or multi-temporal data. By contrast, the conceptual framework proposed by Leyk et al. (2005) suits well to long-term land cover change analysis, as it was based on historical forest cover change investigation in Switzerland. Levk et al. (2005) define the uncertainty in GIS as "the lack of knowledge about:

- objects of the real world due to erroneous measurement, vague definitions and concepts or unknown and ambiguous meaning,
- effects of transformations performed on the data,
- the latter's suitability for the intended appli-

In case of historical maps, each of these aspects of uncertainty refers to one of three inter-related domains:

- production-oriented uncertainty;
- transformation-oriented uncertainty;
- application-oriented uncertainty.

First stage of any map comparison (e.g. in order to detect changes in land-use) is to understand what does a map show, and, equally important, what a map does not show. Being aware of map imprecision and its impact on research results, Leyk et al. (2005) argued that *production-oriented* uncertainty influences change detection analysis

more than two other types. In the first domain, several aspects can be taken into account, e.g. spatial effects related to map production and generalisation or lack of knowledge about historical semantic models employed in mapping. *Transformation-oriented uncertainty* is closely related to processing error (Goodchild 1991) and may be triggered by scanning of paper maps, georeferencing and object extraction. Several aspects of transformation-oriented uncertainty are relatively easy to assess, e.g., accuracy of georeferencing based on control points could be expressed using Root Mean Square Error (RMSE). Application-oriented uncertainty arises due to differences in meanings of objects presented on maps and discrepancies between original and intended use of the maps which in some cases may show an inadequacy of comparison of historical and current data (Leyk et al. 2005).

Each of these three domains contains different aspects of uncertainty which have to be investigated separately. The overall uncertainty assessment aims at answering the question whether the sum of defined uncertainties is acceptable for a specific application.

Historical maps used in the study

In the Polish Carpathians our analysis aims at quantifying the forest cover dynamics over 120 years (mid-19th century - 1970s) starting with the Second Military Survey Map of the Habsburg Empire (scale 1:28,000). The Second Military Survey Map was the first empire-wide topographic map using a proper map projection (Timár 2004, Skaloš et al. 2011, Affek 2013), a generalisation of cadastral mapping (Franciscian Cadaster 1:2,880). The Polish Carpathians are presented on three different editions of the map. The oldest set covers two regions of Polish-Slovak borderland (Spiš and Orava) and was published between 1822-1824 (10 sheets). Additional 8 sheets covering the south-eastern part of Silesia were published between 1839-1940. The main part of the Second Military Survey Map presenting the Polish Carpathians was created between 1861-1862 (112 sheets) and has the highest quality. Regardless the edition, forests were marked in grey colour with a dark boundary outline.

The intermediate data set was the Polish Military Map (WIG) in scale 1:100,000, published between 1934–1938. At the time of creation, the map was considered as an excellent example of the modern cartographic design and valuable source of information (Krassowski 1973). Forest patches were marked in green colour with a dotted boundary line.

The latest data set was the Polish Topographic Map (1:25,000) created between 1975–1983 by the Head Office of Geodesy and Cartography (Główny Urząd Geodezji i Kartografii, GUGIK). Forests were marked in green colour with a dotted boundary line.

All above-mentioned maps have been widely used in land use and land cover change research in the Carpathians (e.g., Kozak 2003, Warcholik 2005, Kaim 2009, Ostafin 2009, Affek 2011). Other datasets, initially taken into consideration, either did not cover the whole study area (e.g., 1930s military maps in scale 1:25,000) or had relatively poor quality (Third Military Survey Map from the late 19th century) and therefore were not included in the analysis.

In the Swiss Alps, the oldest material used in the study was the Dufour Original Survey Map dated between 1845-1864 and created in 1:25,000 scale for the Swiss plateau and 1:50,000 for mountain areas. Forests were presented in green colour, sometimes with an additional dark-green outline. For the end of the 19th century and the mid-20th century two editions of the Siegfried Map were selected. The Siegfried Map is the second federal map series (1870-949), with map sheets in 1:25,000 scale for the Jura and the Central Plateau and in 1:50,000 scale in the Alps. Land use and land cover information includes settlements, roads, forests, wetlands, peatlands, orchards, vineyards and unvegetated areas (glaciers, rocks). Forests were shown with small, thin graphical symbols closely spaced to each other, yielding a stylized kind of tree patterns (Leyk et al. 2006). Forest boundaries were indicated by thin lines whereas open forests were not clearly delineated. All editions of the Siegfried Map are available in a digital form (scanned and georeferenced) and have been used for historical land cover reconstructions (e.g., Gimmi et al. 2011, Ginzler et al. 2011). From 1940 onwards, the modern 'Landeskarte der Schweiz' gradually replaced

the Siegfried Map (Grosjean 1996). In our study, versions compiled and published for 1970s and 2012 were chosen. For 1970s, forested areas were presented in green colour with black, solid line around the patches. For 2012 the map was available in the digital vector format from the Swiss Topographical Office (swisstopo DV033594).

Production-oriented uncertainty

Production-oriented uncertainty covers a wide range of topics of great importance for change detection results. Two aspects seem to be especially important – forest definitions and spatial effects related to cartographic generalisation.

Forest definitions

Defining "forest" is a complex problem (Lund 1999, Bennet 2001), as physical land cover, land use and geometry (e.g., area) are involved. Forest definitions frequently imply a minimum area (see e.g. Ustawa... 1991, Global... 2010). Swiss example shows that forest definition on the Siegfried Map surveys were adopted from Dufour Map (Gugerli, Speich 2002), what means that till mid-20th century forest included also stands of green alder and dwarfpine. On Landeskarte der Schweiz surveys (since mid-20th century onward) forest definition considered slightly different conditions: coverage of trees >50% and height of trees >3 m. Age and use of forest was not considered.

We were not able to find a reliable reference to the original forest definition in the Second Military Survey Map. However, it is important to stress that forest patches were presented according to property boundaries (Troll 2013). Considering the other two Polish maps, forest was understood as a land use, what implies that clear-cuts were not shown. As for the minimum forest area on the oldest map, the smallest forest patch corresponded to land parcels with forest use delineated on the cadastre that was a source for the Second Military Survey Map. The Polish Military Map (1930s) defined forest as a polygon with side length of at least 30 m (Walczak 1946). For topographic maps from the 1970s/1980s, the guidelines defined forest as a polygon larger than

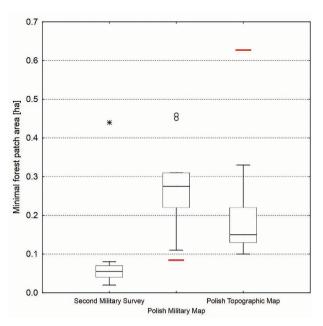


Fig. 1. Minimum forest patches for 10 randomly chosen map sheets for each map set in the Polish Carpathians; lines in red show the value defined by map instruction (not available for the Second Military Survey Map)

 10 mm^2 (0.625 ha in the scale of the map, Instrukcja... 1980).

Testing the materials for the Polish Carpathians, we found that the smallest forest patch on the Second Military Survey Map had 0.02 ha, and 0.5 on average (Fig. 1), on the Polish Mili-

tary Map it was 0.11 ha, very close to the threshold defined by mapping guidelines, and 0.27 on average, and in case of the Polish Topographic Map the smallest forest patch had 0.1 ha, and 0.14 ha on average, exceeding in many instances the threshold specified in the guidelines. The identified smallest forest mapping units reflected both map design rules and the specific landscape patterns at the time, having important consequences for further change analysis.

Spatial effects related to map production and cartographic generalisation

One of the crucial aspects of map creation and design process is cartographic generalisation. This aspect is extremely important in our study as the scale of the Polish Military Map was significantly different to other two maps. However, being aware of the fact that the Polish Military Map was intended to replace the 1:25,000 map where the latter was not available (Przepis... 1929), we hypothesized that it may show spatial detail in a comparable way to maps in larger scale. Therefore we compared forest distribution and simple distance-based measures for 1:100,000 and

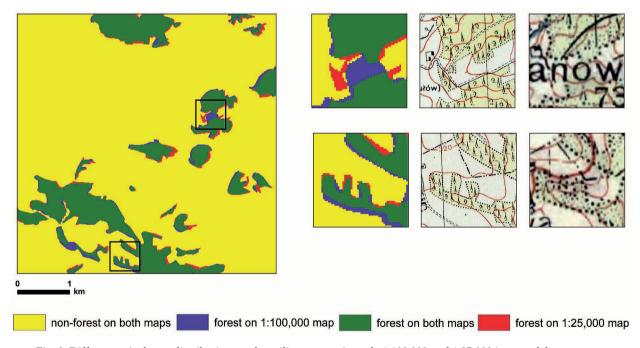


Fig. 2. Differences in forest distribution on the military maps in scale 1:100,000 and 1:25,000 in one of the test areas

	Test area 1		Test area 2	
Map scale	1:25,000	1: 100,000	1:25,000	1: 100,000
(publishing year)	(1935)	(1935)	(1935)	(1934)
No of patches	55	48	21	19
Minimum distance between closest patches [m]	14.80	20.21	28.44	15.63
Average minimum distance between 5 pairs of closest patches [m]	15.92	24.67	61.25	65.17
Forest cover [%]	38.66	38.20	16.08	15.99
Forest cover agreement [%]	89.8		96.8	

Table 1. Forest cover distribution and distance indicators on 1:100,000 and 1:25,000 maps

1:25,000 maps¹ on two 5 × 5 km test sites (Fig. 2, Table 1). Distance between closest patches may be considered as an indicator of cartographic precision and the average distance between five pairs of closest patches corresponds to metrical entropy defined by Bjørke (1996). The results show that forest was mapped on both maps in a relatively consistent way with lower than expected impact of scale-driven generalisation, with surprisingly small differences between 1:100,000 and 1:25,000 maps.

Transformation-oriented uncertainty

Working on historical maps in GIS is always connected with transforming paper data into digital form (Leyk et al. 2005). Several steps of that process may result in uncertainty, in particular geo-referencing and data acquisition.

In our study data acquisition process was based on both manual vectorisation (Second Military Survey Map, Polish Military Map, Dufour Map, two editions of Siegfried Map) and automatic feature extraction (Polish and Swiss maps created in 1970s). The accuracy of automatic feature extraction was found to reach in most cases above 95% (Ostafin et al. in preparation). As for the manual vectorisation, in parallel to data control procedures (i.e. by topology rules and visual verification), independent tests were conducted for two Carpathian maps. The same group of 12 people was asked to vectorise manually the same test areas of the Polish Military Map and the Polish Topographic Map. Their results were

then compared to the forest mask prepared by an expert. The average amount of discrepancies did not exceed 5% in case of the first map and 2% for the latter. Systematic tests were not carried out for the Second Military Survey Map, yet our experiences show that interpretation of forest boundaries is significantly more difficult and subjective for the oldest map editions than for the edition published in 1860s.

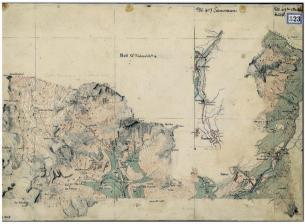
During vectorisation of the Dufour Map a problem of overlapping map sheets (with differences in delineation of forested areas) had to be solved. The base map was chosen taking into account the date of publishing (with preference to the older edition) and map quality (Fig. 3).

Application-oriented uncertainty

Comparison of different map sets is exposed to uncertainty also due to different sematic models standing behind the information we want to compare. It is highly dependent on the intended use of historical maps as well as on the map content taken into consideration. The oldest Carpathian map we used was created for military purposes (reflected e.g. in a complex road network classification), but land use information was obtained by a generalisation of cadastral mapping, implying a similarity of forest patches to parcel boundaries. Although the Polish Military Map had the same objectives, the military operations changed in time and influenced forest delimitation since the mid-19th century. Hence, in the 1930s, forest was perceived rather as a barrier for military troops or as an area for avoiding detection from aerial observation (Instrukcja... 1925). The Polish Topographic Map was intended to provide spatial information for regional

The 1:25,000 map was initiated in 1920s by the Polish Geographic Military Institute, yet only several areas in the Polish Carpathians were mapped before the World War II.





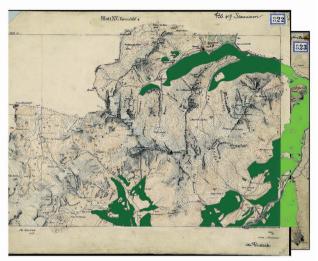


Fig. 3. Overlapping map sheets dating from 1850 (upper left) and 1849 (lower left). Due to quality issues (mapping of a larger continuous area) the overlapping area was mapped from the 1850 map (dark green) while the smaller area on the right side was only depicted on the 1849 map (light green)

planning and for economic purposes, being independent from military mapping. According to the guidelines, forest was understood as a land use and separated from group of trees.

Semantic model difference – a case of Silesia

Our analysis highlighted one specific area (Silesia), where various forest cover patterns were correlated to differences in semantic models of two editions of the Second Military Survey Map (Fig. 4).

In the western part, forest cover was relatively low and significant part of the mountains was covered by forested pastures. In the eastern part of the mountain range mapped 20 years later, the pastures were almost absent and share of forested

land was significantly higher. Possible explanation of the difference might be connected rather to various semantic schemes defining forests and forested pastures in 1840s and 1860s than to real difference in landscape or rapid forest cover increase. As forest definition in the Second Military Survey Map was likely related to ownership patterns inherited from the original cadastral data, it could be significantly altered due to changes in the land ownership following the liberation of peasantry in 1848 (Kozak 2010), and significant reduction of grazing rights in forested areas.

Reliability of change trajectories

The examples above show how uncertainty investigation improves the understanding of the final land cover (or forest) change detection mod-

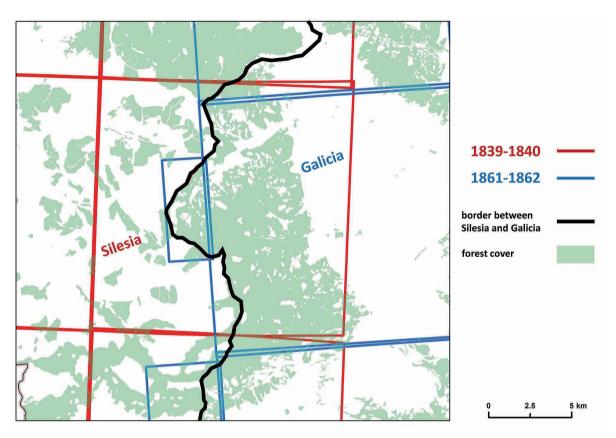


Fig. 4. Differences in forest cover between Silesia and Galicia shown on different editions of the Second Military Survey Map

el. Regardless the source, uncertainty affects reliability of land cover change trajectories. Therefore an alternative way of uncertainty assessment is a trajectory analysis. Its aim is to assess the reliability of a whole map-based time series using proportions of pixels falling into a specific change category. Whether a change category

Table 2. Trajectory analysis for Swiss and Polish parts of the study area (1 – forest, 0 – non-forest)

Trajectory – Swiss Alps (1850–1880–1940–2012)	Portion of forest in 2012	Σ	
1-1-1	48.7%		
0-1-1-1	8.2%	87.8%	
0-0-1-1	7.5%		
0-0-0-1	23.4%		
1-0-0-1	6.9%	94.7%	
1-0-1-1	3.0%	97.7%	
1-1-0-1	1.7%	99.4%	
0-1-0-1	0.6%	100%	
Trajectory – Polish Carpathians (1850–1930–1970)	Portion of forest in 1970	Σ	
1-1-1	54.3%		
0-1-1	15.6%	15.6% 93.6% 23.6%	
0-0-1	23.6%		
1-0-1	6.4%	100%	

is more or less realistic depends on the overall knowledge of the regional land use history. For the Swiss part of the study area, almost 95% trajectories ending as forest in 2012 were found to be very realistic (e.g., stable forest, or change from non-forest to forests either in 1880, 1940 or 2012) or realistic (deforestation in the first period and forest re-growth in the last period), and only 5% represent less realistic trajectories (e.g. non-forest in 1850 and 1940 and forest in 1880 and 2012; Table 2). In the Polish Carpathians the results of similar trajectory analysis show slightly worse results than in Switzerland, as only 93.6% of the trajectories are realistic or very realistic.

While trajectory analysis does not solve all the problems resulting in uncertainty, it helps in quantifying overall consequences of various uncertainties embedded in the map-based change detection.

Discussion and conclusions

Leyk et al. (2005) suggested that the condition of *fitness for use of the data* has to be met in case

of maps to conduct properly the analysis. This condition may be verified assuming that different types of guidelines and reference materials are available. If not, the uncertainty level increases. Unfortunately, *historical geography is rarely data-rich* (Gregory, Ell 2007) which applies especially to the oldest data sets. Hence, alternative methods to assess reliability of old maps are needed.

In this paper we highlighted selected aspects of uncertainty investigation in long-term change detection studies with maps, on a basis of forest cover change analysis in the Polish Carpathians and Swiss Alps. Investigation scheme employed was based on the conceptual framework and three uncertainty domains proposed by Leyk et al. (2005). Each uncertainty domain was analysed separately with results proving that 5-10% errors are inherent at various stages of analysis; in some cases - especially, modification of meanings of specific categories over time - they may put in doubt the results of change analysis if not carefully considered and verified against supplemental information. In other instances, the errors do not necessarily undermine the land cover change analysis: its value depends on the overall uncertainty level that is crucial to accept or reject the final results. In case of our research, preliminary results of trajectory analysis show that in the Swiss Alps only around 5% of mapped areas, and less than 7% in the Polish Carpathians may be considered uncertain, which is an optimistic result for the reliability of forest cover change mapping and further research.

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